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## Single-Co Kondo effect in atomic Cu wires on Cu(111)

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Linear atomic chains containing a single Kondo atom, Co, and several nonmagnetic atoms, Cu, were assembled atom by atom on Cu(111) with the tip of a scanning tunneling microscope. The resulting one-dimensional wires,  $\text{Cu}_m\text{CoCu}_n$  ( $0 \leq m, n \leq 5$ ), exhibit a rich evolution of the single-Co Kondo effect with the variation of  $m$  and  $n$ , as inferred from changes in the line shape of the Abrikosov-Suhl-Kondo resonance. The most striking result is the quenching of the resonance in  $\text{CuCoCu}_2$  and  $\text{Cu}_2\text{CoCu}_2$  clusters. State-of-the-art first-principles calculations were performed to unravel possible microscopic origins of the remarkable experimental observations.

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### I. INTRODUCTION

The Kondo effect was originally observed as the resistivity increase below a characteristic temperature of some metals containing magnetic impurities [1,2]. As intuited by Kondo in 1964, many-body correlations are at the origin of this phenomenon [3,4]. Later, his ideas were extended beyond the perimeter of perturbation theory by Anderson [5,6] and by Wilson [7] understanding and exploiting the role of scale invariance. The conduction electrons of the metal scatter off the local spin of a single quantum impurity and a low-energy collective excitation described by a quantum mechanical singlet wave function is formed. The bare magnetic moment is hence screened and, oversimplifying, one can picture this mechanism as multiple spin flips occurring due to the exchange interaction between the impurity spin and the conduction electrons.

The spectroscopic signature of this spin exchange is represented by the Kondo [3,4] or Abrikosov-Suhl [8–10] resonance at the Fermi energy  $E_F$ . At zero temperature the resonance full width at half maximum is related to the Kondo temperature  $T_K$  via  $k_B T_K$  ( $k_B$  is the Boltzmann constant). The

presence of this resonance was confirmed in photoemission [11–16] and inverse photoemission [17] experiments.

It is certainly no exaggeration to say that the detection of the Abrikosov-Suhl-Kondo (ASK) resonance at the single-impurity level with a scanning tunneling microscope (STM) [18,19] represents a seminal finding in surface physics. In spectra of the differential conductance ( $dI/dV$ ,  $I$  current,  $V$  bias voltage) the ASK resonance appears with a Fano [20,21] or Frota [22,23] line shape. The Fano line shape reflects that spin-conserving tunneling occurs directly from the tip to the conduction electron continuum and indirectly via the Kondo resonance. The interference of tunneling electrons in these two paths leads to the characteristic spectroscopic line shape [18,19]. Many-body numerical renormalization group calculations [24] justify the phenomenological Frota line shape, which was likewise reported from experiments [25,26]. A wealth of reports followed the initial observations [18,19] and revealed the rich physics of the single-atom [27–32] and single-molecule [33–51] Kondo effect. Excellent review articles are available, e.g., Refs. [52–54].

Importantly, variations of the ASK resonance line shape in spectroscopy experiments with an STM serve as a subtle probe for magnetic-interaction [45,55–64], hybridization [32,34–36,65–69], and density-of-states (DOS) [66,70–72] effects. In particular, a nonmonotonic evolution of  $T_K$  of a single Co atom in a compact  $\text{CoCu}_n$  cluster on Cu(111) [66] unraveled that the local electronic structure at the magnetic-impurity site is essential for its Kondo effect, rather than the sheer number of coordinations with nearest-neighbor atoms. Deviating from the previous *compact* cluster geometry [66]

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the evolution of the Kondo effect in *linear*  $\text{Cu}_m\text{CoCu}_n$  clusters is reported here. All atomic chains exhibit ASK resonances with  $40 \leq T_K \leq 110$  K with two surprising and notable exceptions: the ASK resonances at the Co site for  $\text{CuCoCu}_2$  and  $\text{Cu}_2\text{CoCu}_2$  clusters are quenched, at odds with all other clusters that show a clear spectroscopic signature of the Kondo effect.

Motivated by these appealing experimental results, density functional theory (DFT) and quantum Monte Carlo (QMC) calculations were applied in order to describe the Kondo physics of the linear clusters. While many properties of the clusters are captured by the calculations, the atomically fabricated  $\text{Cu}_m\text{CoCu}_n$  clusters define a test case for systematically benchmarking theory against experiment. The reliable description of complex correlated electronic systems presents an outstanding challenge in modern condensed-matter physics. Rigorous benchmarks across methods for the Hubbard model [73] and a hydrogen chain [74] have proven extremely insightful. Benchmarks of correlated phenomena such as Kondo physics in real materials and theory based on state-of-the-art first-principles calculations are virtually absent, however. Consequently, a corresponding high demand exists. Our work serves this purpose: rather than phenomenologically fitting of a single system, calculations are performed on the highest level of theory available for a range of systems without any adjustable parameters throughout this series. As a starting point towards such a benchmarking, DFT and QMC calculations were combined in a “DFT++ manner” [75] to test to which extent experimental findings can or cannot be explained by this approach. Our work unveils the capabilities and open issues of state-of-the-art modeling techniques.

## II. EXPERIMENT

Experiments were performed with an STM operated in ultrahigh vacuum ( $10^{-9}$  Pa) and at 5 K. Cu(111) surfaces were cleaned by  $\text{Ar}^+$  bombardment and annealing. Chemically etched W wires—presumably coated with Cu substrate material due to *in situ* preparation by indentations—served as STM tips. Single Co atoms were deposited at  $\approx 8$  K from an electron beam evaporator through openings of the radiation shields of the bath cryostat. Single Cu atoms were transferred from the tip to the surface by controlled tip-surface contacts [76–79]. STM images were recorded at constant current with the bias voltage applied to the sample. Spectra of  $dI/dV$  were acquired by sinusoidally modulating the bias voltage (1 mV<sub>rms</sub>, 950 Hz) and measuring the first harmonic of the current response of the tunneling junction with a lock-in amplifier. Topographic data were processed using WSXM [80].

## III. RESULTS AND DISCUSSION

### A. Scanning tunneling microscopy and spectroscopy

Figure 1 shows representative STM images of the  $\text{Cu}_m\text{CoCu}_n$  clusters studied in this work. In the following these assemblies will be referred to as  $(m, n)$  clusters. Single Co [Fig. 1(a)] and Cu atoms on Cu(111) appear as circular protrusions with larger apparent height for Co ( $\approx 70$  pm) compared to Cu ( $\approx 50$  pm) at  $V = 10$  mV. The  $(m, n)$  clusters

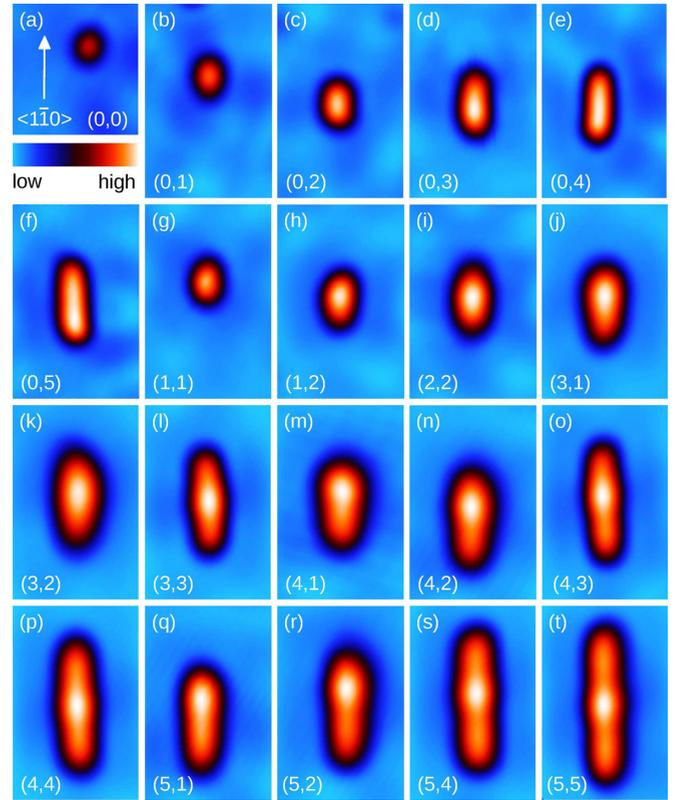


FIG. 1. STM images of atom-by-atom fabricated linear  $\text{Cu}_m\text{CoCu}_n$  clusters on Cu(111) denoted  $(m, n)$  with  $0 \leq m, n \leq 5$  (bias voltage: 10 mV, tunneling current: 50 pA). (a) STM image of a single Co atom (size:  $2.6 \times 2.7$  nm<sup>2</sup>). A Cu(111) crystallographic direction  $\langle 1\bar{1}0 \rangle$  is indicated by an arrow. The color scale ranges from 0 (low) to 120 pm (high) in all STM images. (b)–(t) STM images of linear clusters ( $2.6 \times 4$  nm<sup>2</sup>).

were fabricated atom by atom [81,82]. After assembling the linear  $\text{Cu}_m$  cluster, one edge of the chain was decorated by a single Co atom. Additional  $n$  Cu atoms were then attached to this Co atom, continuing the direction of the chain. Attaching a single Cu atom to Co [Fig. 1(b)] increases the Co apparent height to  $\approx 90$  pm. (0,2) clusters [Fig. 1(c)] exhibit a Co apparent height of  $\approx 110$  pm. Additional Cu atoms in  $(0, n)$  clusters ( $n \geq 3$ ) do not change the Co apparent height appreciably [Figs. 1(d)–1(f)]. Similar observations hold for  $(m, n)$  clusters with  $m \geq 1$  [Figs. 1(g)–1(t)]. Inside such clusters Co always appears  $\approx 15$  pm higher than its Cu neighbors. All linear atomic chains are aligned with  $\langle 1\bar{1}0 \rangle$  crystallographic directions of Cu(111) [arrow in Fig. 1(a)].

The one-dimensional wires were used to explore changes in the Co Kondo effect. Spectra of  $dI/dV$  are summarized in Fig. 2 for  $(0, n)$  clusters ( $0 \leq n \leq 5$ ) in Fig. 2(a) and for  $(m, n)$  clusters ( $1 \leq m, n \leq 5$ ) in Fig. 2(b). All spectra were acquired atop the Co central region. The majority of spectra exhibits an indentation close to zero bias voltage, which is interpreted as the ASK resonance. Solid lines are fits to the data using the function  $f(V) + p(V)$  with the Fano line shape  $f(V) = a(q + \varepsilon)^2 / (1 + \varepsilon^2)$  [ $a$  is amplitude,  $q$  is asymmetry parameter,  $\varepsilon = \beta(eV - \varepsilon_0)$  with  $1/\beta = k_B T_K$ ,  $e$  is the elementary charge, and  $\varepsilon_0$  is the resonance energy] and a linear background

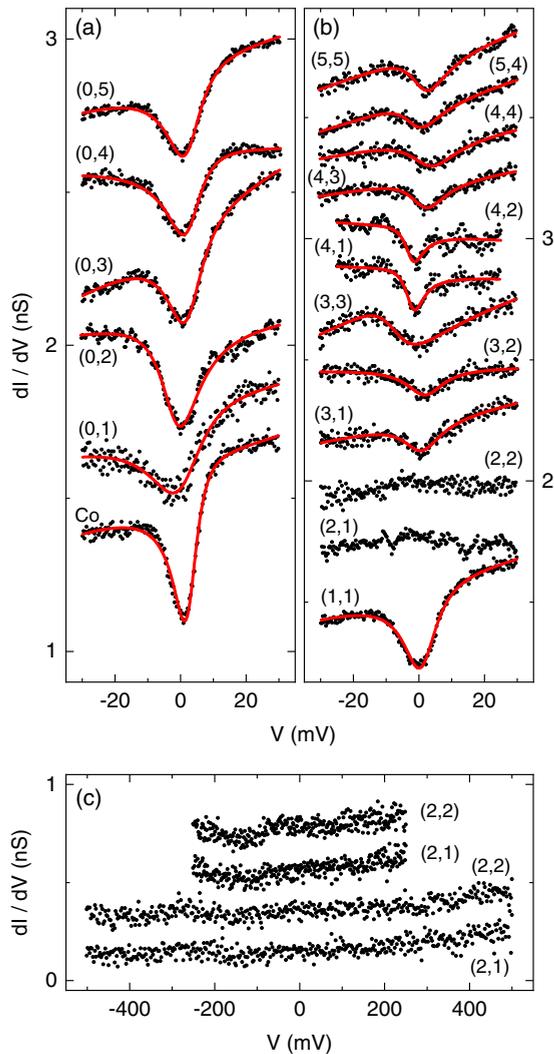


FIG. 2. Spectroscopy of the ASK resonance. Spectra of  $dI/dV$  (dots) recorded above the Co atom in  $(m, n)$  clusters on Cu(111) for (a)  $m = 0, n \geq 1$  and (b)  $m, n \geq 1$ . The bottom spectrum of (a) depicts the single-Co ASK resonance. Solid lines are fits to the data using the Fano line shape (see text). Spectra are offset for clarity. Individual spectra without vertical offset are presented in the Supplemental Material [83]. Feedback loop parameters prior to data acquisition: 30 mV, 50 pA. (c) Spectroscopic data recorded above the Co atom in (2,1), (2,2) clusters in wide bias voltage ranges. Feedback loop parameters prior to data acquisition: 200 mV (top pair), 500 mV (bottom pair), 50 pA.

$p(V) = b_0 + b_1V$ . A linear background was previously used in many analyses of the ASK resonance line shape [52–54]. It may be justified by the voltage-dependent transmission of the tunneling barrier that was reported in a theoretical work considering all three dimensions of the barrier and the different atomic orbitals of tip and sample [84]. While the transmission was demonstrated to evolve in a nonlinear manner for bias voltages on the order of 1 V and differently for the investigated  $s, p, d$  atomic orbitals, in a small range around 0 V, which is particularly interesting for the spectral line shape of the ASK resonance, the transmission and, thus, the background in  $dI/dV$  data may well be described by a linear

TABLE I. Kondo temperature  $T_K$  (K) of  $(m, n)$  clusters extracted from fits of  $dI/dV$  spectra using the Fano line shape and a linear background.

$(m, n)$	0	1	2	3	4	5
0	$51 \pm 2$	$112 \pm 7$	$82 \pm 2$	$77 \pm 2$	$77 \pm 2$	$75 \pm 2$
1	$112 \pm 7$	$71 \pm 2$	–	$80 \pm 7$	$38 \pm 3$	
2	$82 \pm 2$	–	–	$79 \pm 7$	$39 \pm 5$	
3	$77 \pm 2$	$80 \pm 7$	$79 \pm 7$	$110 \pm 8$	$74 \pm 5$	
4	$77 \pm 2$	$38 \pm 3$	$39 \pm 5$	$74 \pm 5$	$96 \pm 10$	$77 \pm 6$
5	$75 \pm 2$				$77 \pm 6$	$76 \pm 5$

function whose slope depends on the contribution of the actual atomic orbitals involved in the tunneling. Striving moreover for a reliable comparison of extracted Kondo temperatures, the spectroscopic data of all clusters were fit in the same bias voltage range,  $-30 \text{ mV} \leq V \leq 30 \text{ mV}$ . The Frota line shape superimposed on a linear background was likewise used to fit the experimental data. However, the fit results were inferior to the results obtained with the Fano line shape. Therefore, in this work all ASK resonance  $dI/dV$  data were fit with the Fano line shape combined with a linear background.

The single Co atom [bottom data set of Fig. 2(a)] exhibits an ASK resonance with a width that corresponds to  $T_K = 51 \pm 2 \text{ K}$  (see Table I for a collection of all extracted  $T_K$ ), which is in agreement with previous reports [28,66]. By adding one Cu atom [(0, 0)  $\rightarrow$  (0, 1)]  $T_K$  increases by more than a factor 2 to  $T_K = 112 \pm 7 \text{ K}$ . This increase of  $T_K$  is in accordance with a previous work on compact  $\text{CoCu}_n$  clusters [66]. The addition of a second Cu atom [(0, 1)  $\rightarrow$  (0, 2)] gives rise to a considerable decrease of  $T_K$  to  $82 \pm 2 \text{ K}$ . For  $(0, n)$  clusters ( $n \geq 3$ )  $T_K$  then stays nearly constant. The value of  $T_K = 77 \pm 2 \text{ K}$  for (0,3), (0,4) clusters agrees well with previous experimental observations and calculations for linear  $\text{CoCu}_3$  and  $\text{CoCu}_4$  clusters [60].

Clusters  $(m, n)$  with  $m, n \geq 1$  unveil unexpected behavior. The most remarkable observation is the entire quenching of the ASK resonance of Co in (1,2), (2,1), (2,2) clusters [second and third spectrum counted from the bottom in Fig. 2(b)]. This behavior was reproduced for several clusters and tips. The suitability of the tip for spectroscopic measurements was intermediately controlled by reproducing the single-Co ASK resonance and the steplike onset of the Cu(111) Shockley surface state (not shown). In order to exclude the presence of exceptionally wide ASK resonances [30] which would appear rather flat on the small bias voltage range of Fig. 2(b), the bias voltage range in  $dI/dV$  spectroscopy was extended up to  $\pm 500 \text{ mV}$  [Fig. 2(c)]. An ASK resonance was not observed.

Moreover, for the larger clusters a maximum of  $T_K$  was reached in the symmetric case, i.e., for (3,3) clusters with  $T_K = 110 \pm 8 \text{ K}$  and for (4,4) clusters with  $T_K = 96 \pm 10 \text{ K}$ . In both cases, the addition of a single Cu atom to one side of the linear chain leads to a significant drop of  $T_K$ ,  $T_K = 74 \pm 5 \text{ K}$  for (3,4) clusters. (4,5), (5,5) clusters do not adhere to this trend, which may indicate that these very long clusters behave like infinite Cu chains with an embedded Co atom. The asymmetry parameter  $q$  varied between  $-0.2$  and  $0.2$

for all clusters exhibiting an ASK resonance without showing characteristic behavior with  $m$  and  $n$ .

Before turning to the calculations it is important to mention that changes in  $T_K$  observed from the small linear clusters reported here deviate from the previously reported evolution of  $T_K$  in compact  $\text{CoCu}_n$  clusters [66]. Indeed, for compact  $\text{CoCu}_n$  clusters  $T_K$  was demonstrated to first increase with  $n$  up to  $n = 2$  with a maximum value  $T_K \approx 326$  K and then decrease down to  $T_K \approx 43$  K for  $n = 4$ . In contrast, the short linear clusters discussed here reach a maximum of  $T_K$  for (0,1). Increasing the number of Cu atoms by one leads to a nearly halved  $T_K$  for (1,1). Obviously the Co coordination number in compact  $\text{CoCu}_2$  and linear  $\text{CuCoCu}$  clusters is identical. However, the different behavior of  $T_K$  in the two cases evidences the impact of the actual cluster geometry on the Kondo effect.

## B. Model calculations

### 1. Density functional theory

Simulations of the  $(m, n)$  clusters were performed on Cu(111) slabs with a lateral extent of  $3 \times 13$  unit cells. For calculations of the geometrical structure three Cu layers were used, while for the hybridization simulations five Cu layers were included. The calculations are based on the Vienna *ab initio* simulation package (VASP) [85] with the projector augmented wave (PAW) basis sets [86,87] and the generalized gradient approximation (GGA) to the exchange correlation potential [88].

*Atomic structure and magnetic moment formation.* We first investigated the atomic structure of the adsorbed linear  $(m, n)$  clusters and its dependence on magnetic moment formation by comparing structural relaxations and total energies as resulting from non-spin-polarized (nsp) and spin-polarized (sp) calculations. To obtain an indication for the matching between the fully relaxed geometries in theory and the experimental clusters the evolution of  $dI/dV$  spectra at elevated bias voltage is compared with the calculated DOS (Fig. 3). Figure 3(a) shows the spectroscopic signature of an unoccupied resonance above the Co site in  $(m, n)$  clusters with increasing (from bottom to top) cluster length. The resonance peak shifts to lower bias voltage with increasing  $m$  and  $n$ . Calculations of the local DOS at the Co site [Fig. 3(b)] reveals an unoccupied Co  $p_z$  resonance whose onset likewise shifts to lower energy with increasing cluster size. Owing to the same trend and to similar onset energies [Fig. 3(c)] the peaks in  $dI/dV$  spectra are assigned to the spectroscopic signature of the calculated Co  $p_z$  resonance. Thus, the experimental and calculated evolutions of spectra at elevated energy are consistent, as expected for relaxed geometries.

Side and top views of the calculated clusters are depicted in Fig. 4(a). The chains are almost perfectly linear with only slight vertical ( $< 10$  pm) and lateral ( $< 20$  pm) corrugations. The adsorption heights, Co magnetic moments, and total energy differences between nonmagnetic and magnetic calculations are summarized in Table II. The general trend in all systems under consideration is that the formation of magnetic moments on the order of  $2 \mu_B$  ( $\mu_B$  is the Bohr magneton) is favorable by energies on the order of  $\approx 0.5$  eV and associated

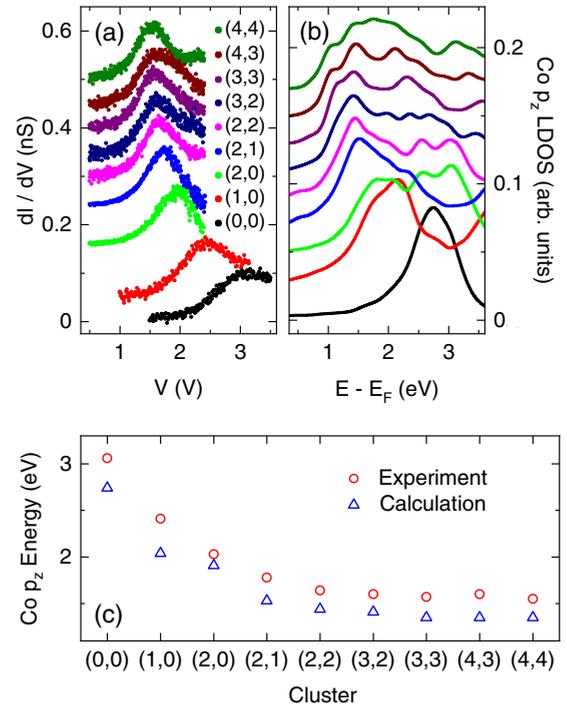


FIG. 3. Evolution of the unoccupied Co  $p_z$  resonance with the cluster size. (a)  $dI/dV$  spectra of an unoccupied state recorded above Co in  $(m, n)$  clusters ( $0 \leq m, n \leq 4$ ). Spectra are vertically offset for clarity. Spectroscopic data without vertical offset are presented in the Supplemental Material [83]. (b) Calculated Co  $p_z$  DOS in  $(m, n)$  clusters. (c) Experimental (circles) and calculated (triangles) unoccupied resonance energy at the Co site in  $(m, n)$  clusters.

with an upward relaxation of the Co atoms on the order of 10 pm.

A direct comparison of total energies without and with spin polarization as a function of adsorption height of the Co atoms in  $(m, n)$  clusters is shown in Fig. 4(b). We find that all clusters favor local magnetic moment formation around the Co sites regardless of structural relaxation details. Consequently, all  $(m, n)$  clusters considered here are potential Kondo systems, including (1,2), (2,1), (2,2) clusters for which an ASK resonance is not discernible in the experiments [Fig. 2(b)].

*Electronic structure in GGA and effective Anderson model.* To investigate possible Kondo physics in the structures at hand, multiorbital Anderson impurity models (AIM) were derived describing the  $(m, n)$  clusters from the DFT-GGA calculations, where electronic correlations arise in the five Co  $d$  orbitals, i.e.,

$$H_{\text{AIM}} = \sum_k \varepsilon_k c_k^\dagger c_k + \sum_{k,\alpha} (V_{k\alpha} c_k^\dagger d_\alpha + \text{H.c.}) + H_{\text{loc}}, \quad (1)$$

with

$$H_{\text{loc}} = \sum_\alpha \varepsilon_\alpha d_\alpha^\dagger d_\alpha + \frac{1}{2} \sum_{\alpha_1, \dots, \alpha_4} U_{\alpha_1, \dots, \alpha_4} d_{\alpha_1}^\dagger d_{\alpha_2}^\dagger d_{\alpha_3} d_{\alpha_4}. \quad (2)$$

Here the operators  $d_\alpha$  ( $d_\alpha^\dagger$ ) annihilate (create) electrons in Co  $d$  orbitals characterized by orbital and spin quantum numbers  $\alpha$ , with corresponding on-site energies  $\varepsilon_\alpha$ , and local Coulomb interactions  $U_{\alpha_1, \dots, \alpha_4}$ . This impurity is embedded in a sea of

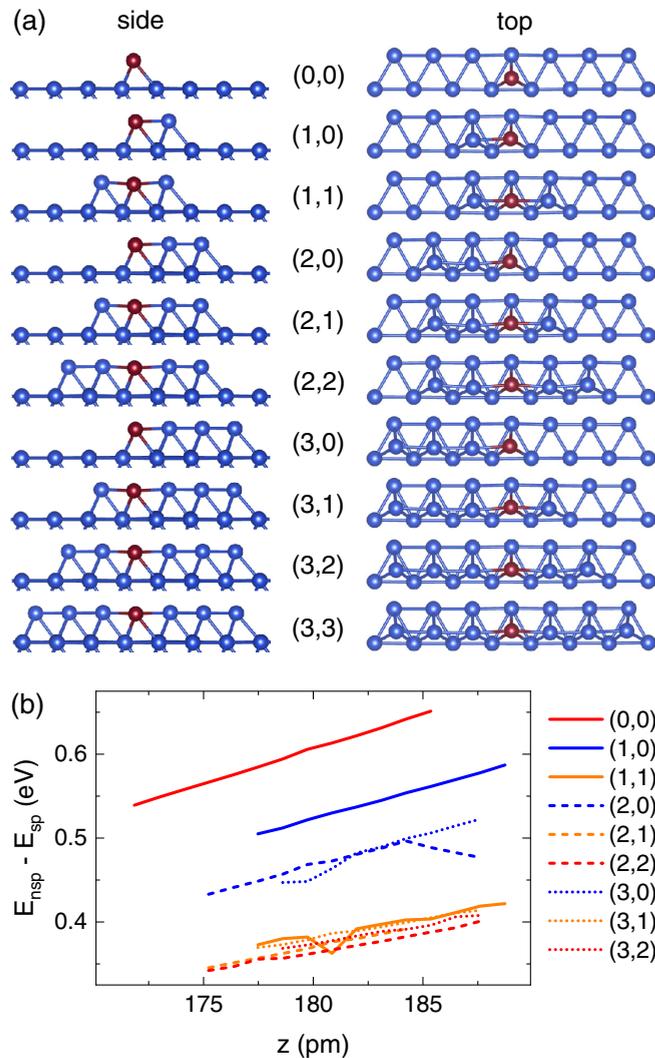


FIG. 4. Simulation of  $(m, n)$  cluster geometry on Cu(111) and comparison of total energies. (a) Side and top view of the relaxed chain structures as obtained from spin-polarized calculations (Cu: blue; Co: red; in the top view only Cu surface atoms closest to the linear chain are shown). (b) Total energy differences  $E_{\text{nsp}} - E_{\text{sp}}$ , of nonmagnetic and magnetic solution for fixed geometries interpolating between the non-spin-polarized (nsp) and spin-polarized (sp) structures. The height  $z$  of the Co atom above the Cu surface is chosen as interpolation coordinate, where the lowest (highest)  $z$  value for each curve corresponds to the structure obtained from the non-spin-polarized (spin-polarized) relaxation.

conduction electron states originating from the surrounding Cu atoms and is described by annihilation (creation) operators  $c_k$  ( $c_k^\dagger$ ) and dispersions  $\varepsilon_k$ , where  $k$  includes crystal momentum, band index, and spin. The coupling between the impurity and the conduction electrons is provided by the hybridization  $V_{k\alpha}$ .

In the AIM only the impurity site is subject to an interaction term, while the bath of conduction electrons is assumed to be noninteracting. The bath degrees of freedom can thus be integrated out and the local electronic properties of the impurity can be described by  $H_{\text{loc}}$  and the hybridization

TABLE II. Adsorption height of Co above Cu(111) for relaxation without (nsp),  $z_{\text{Co}}^{\text{nsp}}$ , and with (sp),  $z_{\text{Co}}^{\text{sp}}$ , spin polarization. The magnetic moment of Co,  $\mu_{\text{Co}}$ , in units of the Bohr magneton  $\mu_B$  originates from all Co electrons.  $E_{\text{nsp}} - E_{\text{sp}}$  denotes the total energy difference between nonmagnetic and magnetic solutions.

$(m, n)$	$z_{\text{Co}}^{\text{nsp}}$ (pm)	$z_{\text{Co}}^{\text{sp}}$ (pm)	$\mu_{\text{Co}}$ ( $\mu_B$ )	$E_{\text{nsp}} - E_{\text{sp}}$ (eV)
(0,0)	172	185	1.99	0.61
(1,0)	178	188	1.90	0.41
(1,1)	179	182	1.80	0.34
(2,0)	179	187	1.94	0.46
(2,1)	179	185	1.86	0.41
(2,2)	180	186	1.79	0.31
(3,0)	179	187	1.88	0.37
(3,1)	179	187	1.79	0.32
(3,2)	179	187	1.79	0.31
(3,3)	180	187	1.79	0.31

function

$$\Delta_{\alpha_1\alpha_2}(\omega) = \sum_k \frac{V_{k\alpha_1}^* V_{k\alpha_2}}{\omega + i\Gamma - \varepsilon_k}, \quad (3)$$

with the effective broadening  $\Gamma$ . We calculated  $\Delta_{\alpha_1\alpha_2}(\omega)$  from first-principles following Refs. [89,90]. The orbital and spin diagonal elements of the hybridization function on Matsubara frequencies ( $\omega + i\Gamma \rightarrow i\omega_n$ ) will enter the QMC simulations presented in the section below. For a first qualitative overview of the hybridization strength, which is one of the determining factors for the occurrence of the Kondo effect and associated with  $T_K$ , we show the orbitally averaged hybridization functions  $\Delta(\omega) = \frac{1}{10} \sum_{\alpha} \Delta_{\alpha\alpha}(\omega)$  with an effective broadening of  $\Gamma = 0.31$  eV for all systems under consideration in Figs. 5(a) and 5(b). The specific choice of  $\Gamma$  is motivated by the sufficient broadening of  $\Delta$ , which otherwise ( $\Gamma < 0.31$  eV) would exhibit strongly peaked variations in  $\omega$  making comparisons for the different clusters [Fig. 5(a)] difficult.

While the hybridization functions differ between the individual chain realizations in several details, a few overarching statements can be made. First and foremost, the magnitude of the hybridization function and also the overall shape is similar in all cases and in line with the hybridization function found for Co atoms on Cu(111) from Ref. [91]. On a very rough qualitative level we would thus expect similar  $T_K$  across the whole range of  $(m, n)$  clusters.

Regarding variations between the different chain structures, we find an increase in hybridization with coordination number of the Co atoms, as one expects. A scaling analysis [92,93] suggests that  $T_K$  depends on hybridization  $\Delta = \Delta(E_F)$  and local interaction  $U$  according to

$$T_K \propto \exp \left[ -\frac{\pi U}{\gamma |\text{Im} \Delta(E_F + i0^+)|} \right], \quad (4)$$

where  $\gamma$  is a factor depending on orbital degeneracies. Therefore, increasing  $|\text{Im} \Delta(E_F + i0^+)|$  should result in (strongly) increasing  $T_K$ . Figure 5(c) shows the measured  $T_K$  in relation to the calculated average hybridization function  $|\text{Im} \Delta(E_F + i0^+)|$ . There is no clear correlation between  $|\text{Im} \Delta(E_F + i0^+)|$  and  $T_K$ . On the contrary, the (2,2) cluster, which displays

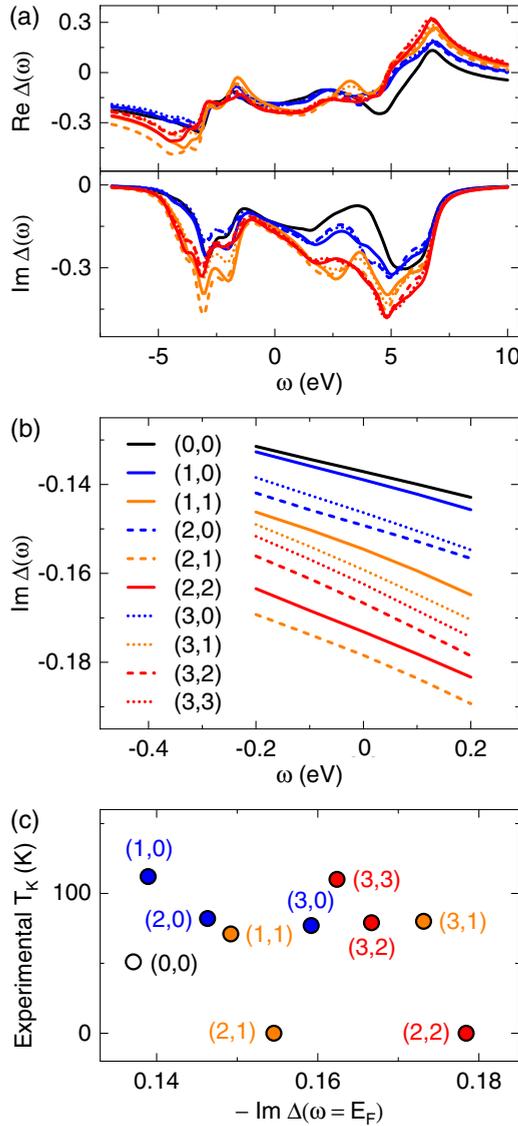


FIG. 5. Orbitaly averaged hybridization functions  $\Delta$  and correlation with  $T_K$ . (a) Real (top) and imaginary (bottom) parts of  $\Delta(\omega)$  for the Co  $d$  orbitals in the different  $(m, n)$  clusters on Cu(111). The legend is presented in (b). (b) Close-up view of  $\text{Im}\Delta(\omega)$  for energies around  $E_F$ . (c) Experimentally extracted  $T_K$  versus  $-\text{Im}\Delta(E_F)$  where each data point corresponds to one  $(m, n)$  cluster.

no signature of the Kondo effect in the experiments, has the largest  $|\text{Im}\Delta(E_F + i0^+)|$  among all systems of this study. We thus conclude that mechanisms beyond this simple orbitaly independent model should be at work in determining the Kondo physics at least in these two special cases.

In order to account for the complex interplay of charge, orbital, and spin fluctuations we now turn to QMC simulations of the full AIM with *ab initio* derived hybridization functions.

## 2. Quantum Monte Carlo simulations

Using the implementation of continuous-time QMC in hybridization expansion (CT-HYB) [94,95] contained in the package w2dynamics [96], we solve the AIM given in Eqs. (1) and (2) numerically exactly. The energy levels of the bath, its

hybridization with the impurity, encoded in the hybridization function of Eq. (3), and the energy differences between the local levels are taken from the DFT-GGA calculations presented in the previous section. We neglect the off-diagonal elements of the hybridization as they are of small magnitude. The fully spherically symmetric local Coulomb interaction tensor  $U_{\alpha_1, \dots, \alpha_4}$  was generated from interaction parameters determined using the constrained random phase approximation for simple surfaces [97,98]. While the systems under investigation are Co atoms in varying surface environments, deviations from spherical symmetry may be neglected due to their minor effects on numerical results for 3d electrons [99]. The chemical potential was chosen to reach an occupation of 8 electrons in the Co  $d$  shell.

To put our approach into context of similar *ab initio* based approaches, e.g., Refs. [66,89–91], we emphasize that we solve the Anderson impurity model with full rotationally invariant Coulomb interaction statistically exactly at unprecedentedly low temperatures. Neglecting interactions beyond those of density-density type would lead to a different position and width of the ASK resonance and, therefore, to erroneous estimates for the Kondo temperature [100].

We use various indicators for the occurrence of the Kondo effect. One is the behavior of the imaginary part of the self-energy at low frequencies (the so called “first Matsubara rule”) [101]. This, together with the calculated quasiparticle weights and scattering rates, does not seem to allow a clear distinction of the chains exhibiting the Kondo effect experimentally from the others.

Another way of judging the propensity of exhibiting the Kondo effect is the direct inspection of the spectral function  $A(\omega) = -\frac{1}{\pi} \text{Im}G_R(\omega)$ . Owing to the CT-HYB algorithm,  $A(\omega)$  includes all local electronic correlation effects beyond DFT. The full Green’s function on the imaginary (discrete) Matsubara frequency axis obtained from CT-HYB was transformed to the retarded Green’s function  $G_R(\omega)$  on the real (continuous) frequency axis using the maximum-entropy method [102–104]. According to Fig. 6, even considering many-body effects, chains that in the experiment have qualitatively different Kondo effects, behave quite similarly in theory. In particular, the (0,2), (1,2), (2,2) clusters display a very similar orbital structure of the Kondo peaks, in spite of the fact that experimentally the first one is the only Kondo-active chain.

For a quantitative comparison between the experimentally extracted widths of the ASK resonance (corresponding to the experimental  $T_K$ ) and the theoretical results we calculate the orbital-renormalized resonance width  $Z\text{Im}\Delta_\alpha(0)$  [91,105,106] where  $Z$  is the quasiparticle weight defined below and relate it to a temperature scale by

$$T_{K,\alpha} = -\frac{\pi}{4} Z\text{Im}\Delta_\alpha(0). \quad (5)$$

This orbitaly dependent measure does not straightforwardly relate to the Kondo temperature of the multiorbital system. However,  $T_{K,\alpha}$  directly measures the width of the *theoretical* resonances and, therefore, represents a natural candidate to compare to the experimentally extracted  $T_K$ , which measures the width of the *experimental* resonances.

The quasiparticle weight  $Z$  was calculated from the imaginary part of  $\Sigma(i\omega_j)$ , the Matsubara self-energy, as

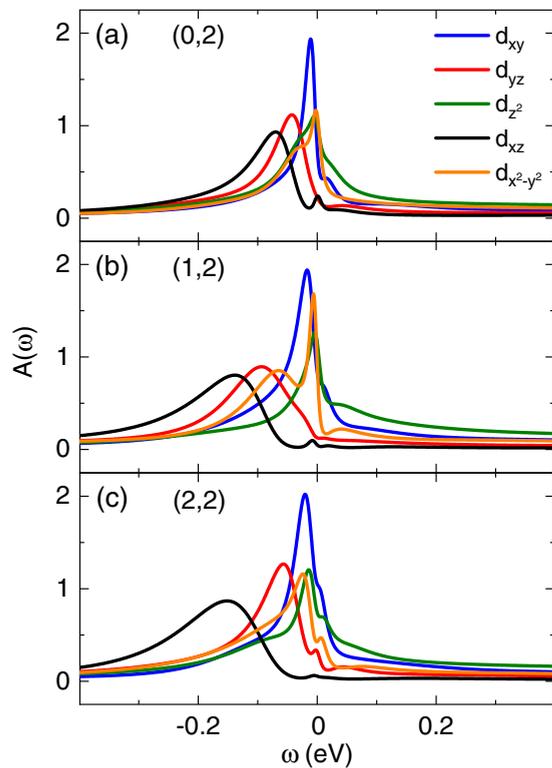


FIG. 6. Comparison of orbitally resolved spectral functions. Spectral functions  $A(\omega)$  obtained for Co  $d$  orbitals using the maximum entropy method from QMC simulations performed for  $(m, n)$  clusters with (a)  $m = 0, n = 2$ ; (b)  $m = 1, n = 2$ ; and (c)  $m = 2 = n$  at a temperature of 46 K.

$Z = [1 - \partial_{\omega_j} \text{Im}\Sigma(i\omega_j)]^{-1}$  in the limit of vanishing  $i\omega_j$  ( $j$  is the index of discrete frequency). In this way,  $T_{K,\alpha}$  may be calculated for each Co  $d$  orbital in the  $(m, n)$  clusters for which QMC simulations were performed. Figure 7 demonstrates that except for the cases in which no ASK resonance was observed experimentally, the calculated orbital-averaged  $T_{K,\alpha}$  [Eq. (5)] never deviates from experimental values by more than a factor 2. Below we show that the orbital-dependent  $T_{K,\alpha}$  reacts sensitively to changes of some model parameters,

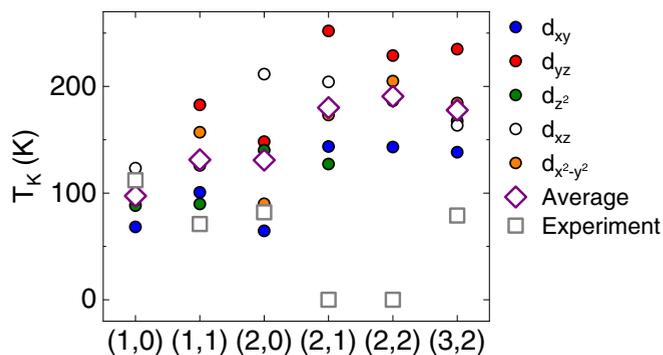


FIG. 7. Orbitally resolved (dots) and averaged (lozenges) renormalized resonance width  $T_{K,\alpha}$  for several  $(m, n)$  clusters and comparison with experimental data (squares). The quasiparticle weight (see text) was calculated in the QMC simulations for each Co  $d$  orbital and averaged. The uncertainty margin of the calculated average spans the orbital variation, against which the statistical uncertainty is small.

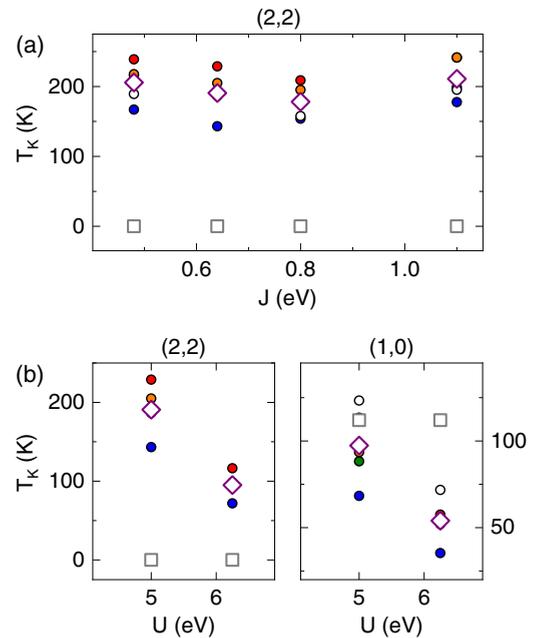


FIG. 8. Orbitally resolved (dots) and averaged (lozenges)  $T_{K,\alpha}$  of  $(2,2)$ ,  $(1,0)$  clusters from QMC quasiparticle-weight calculations and comparison with experimental  $T_K$  (squares). (a) Dependence of  $T_{K,\alpha}$  of a  $(2,2)$  cluster on the Hund coupling constant  $J$  for a Hubbard  $U = 5$  eV. (b) Dependence of  $T_{K,\alpha}$  of a  $(2,2)$  cluster (left) and a  $(1,0)$  cluster (right) on  $U$  for  $J = 0.64$  eV. Uncertainty margins of the calculated average  $T_{K,\alpha}$  reflect the  $T_{K,\alpha}$  variations of the individual Co  $d$  orbitals. The dependence on  $J$  (a) is nearly negligible while the dependence on  $U$  and (b) has roughly the same effect on the orbitally averaged value of both systems. The legend is the same as in Fig. 7.

which may be the origin of discrepancies between theory and experiment.

Experimentally relevant parameters of the AIM—the intraorbital Hubbard interaction  $U$  and the interorbital Hund coupling  $J$ —were varied in order to explore the sensitivity of  $T_{K,\alpha}$  to these parameters. The representative example of a  $(2,2)$  cluster shows that  $T_{K,\alpha}$  responds weakly to variations of  $J$  [Fig. 8(a)]. Increasing  $J$  from 0.48 to 1.10 eV using  $U = 5$  eV, the average of  $T_{K,\alpha}$  over all Co  $d$  orbitals varies slightly between 170 and 211 K. The response of  $T_{K,\alpha}$  to changes in  $U$  is somewhat stronger as shown in Fig. 8(b) for  $(2,2)$  clusters (left) and  $(1,0)$  clusters (right). Using  $J = 0.64$  eV and increasing  $U$  from 5 to 6.25 eV leads to a decrease of the averaged  $T_{K,\alpha}$  from 170 to 95 K for  $(2,2)$  clusters and from 97 to 54 K for  $(1,0)$  clusters, i.e., by roughly a factor 2 in both cases.

A final test was carried out to explore the dependence of  $T_{K,\alpha}$  on variations of the Co adsorption height by  $\pm 10$  pm. The response of the entire spectral function and, in particular, of the ASK resonance energy to vertical displacements of the Co atom in the chains, is quantitatively different for  $(m, n)$  clusters. Figure 9 shows that while quantitative changes in  $T_{K,\alpha}$  of individual orbitals are not the same, the averaged values exhibit very similar behavior for the different clusters. Moreover, a simple relation to the experimental  $T_K$  is not easy to recognize.

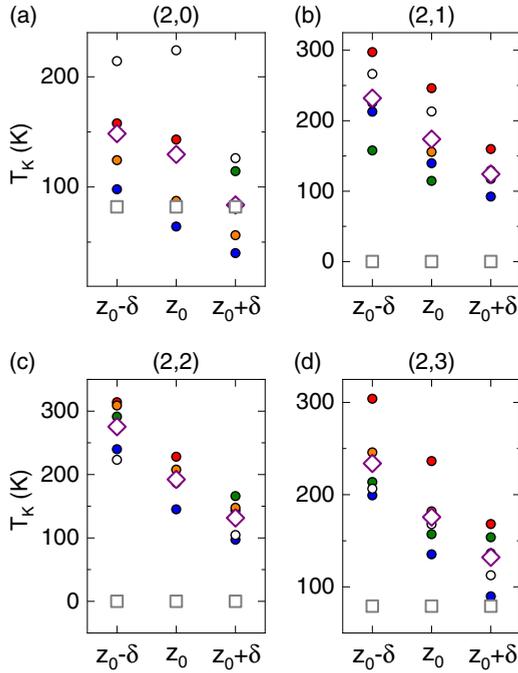


FIG. 9. Orbitally resolved (dots) and averaged (lozenges)  $T_{K,\alpha}$  of (a) (2,0), (b) (2,1), (c) (2,2), and (d) (2,3) clusters from QMC quasiparticle-weight calculations and comparison with experimental  $T_K$  (squares). The plots depict the dependence of  $T_{K,\alpha}$  on variations of the relaxed Co adsorption height  $z_0$  by  $\pm\delta$ . The uncertainty margins of the average  $T_{K,\alpha}$  reflect the  $T_{K,\alpha}$  variations of the individual Co  $d$  orbitals, against which the statistical uncertainty is small. The dependence of the orbitally averaged value on the Co adsorption height is nearly the same for all considered clusters. The legend is the same as in Fig. 7.

#### IV. CONCLUSION

Scanning tunneling spectroscopy of atom-by-atom assembled linear  $\text{Cu}_m\text{CoCu}_n$  ( $0 \leq m, n \leq 5$ ) clusters on Cu(111) reveals rich Kondo physics of the Co atom. Describing the ASK resonance with a Fano line shape unravels a wide range of  $T_K$  from  $\approx 40$  to  $\approx 110$  K depending on  $m$  and  $n$ . Most strikingly, for  $\text{CuCoCu}_2$  and  $\text{Cu}_2\text{CoCu}_2$  the ASK resonance is entirely quenched hinting at the collapse of the Kondo effect.

DFT and QMC calculations indicate the presence of ASK resonances in the spectral functions of all linear clusters. From calculations for the different geometries estimates of  $T_K$  range between  $\approx 100$  and  $\approx 200$  K. Under moderate variations of the interaction parameters or the height of the Co atom, the range of estimates extends further in both directions. The simulations thus capture  $T_K$  qualitatively correctly for the majority of clusters. There are, however, clear deviations of the theoretical from the experimental results. First, the variations of  $T_K$  between the different clusters is not correctly accounted for by the current level of theory. The most remarkable deviation is the presence of an ASK resonance for  $\text{CuCoCu}_2$

and  $\text{Cu}_2\text{CoCu}_2$  in the simulations, clearly contradicting the experimental findings.

In order to identify the origin of these deviations several experimentally relevant model parameters, i.e., the electron-electron coupling strength in the Coulomb tensor, the Co orbital occupation, and the Co atom adsorption height, were varied. The qualitative response of the orbitally averaged  $T_K$  is similar for all clusters suggesting that the experimentally observed absence of the ASK resonance for  $\text{CuCoCu}_2$  and  $\text{Cu}_2\text{CoCu}_2$  is neither of simple electronic nor structural origin. Rather, the microscopic explanation of the quenched ASK resonance in  $\text{CuCoCu}_2$  and  $\text{Cu}_2\text{CoCu}_2$  may involve the increased size of the supercell for simulations, the transmission function to the tip, electron-phonon coupling, and an enlarged basis set for the description of low-energy, spin-orbit interaction and other relativistic effects.

From a methodological modeling standpoint, our results demonstrate that the complexity encoded in nanosystems like adsorbed atoms or clusters on surfaces combined with electronic correlation effects is substantial. It presents a partially solved problem as regards quantitative aspects such as the occurrence of Kondo physics in most systems studied here and a generally qualitatively correct match between experimental and theoretical  $T_K$ . In our view, the investigated linear  $\text{Cu}_m\text{CoCu}_n$  ( $0 \leq m, n \leq 5$ ) clusters on Cu(111) can serve as a very informative benchmark case for the future development of theoretical approaches to correlated nanosystems.

Moreover, the approach presented here may become important for describing Kondo screening in superconductors, which is relevant to topological quantum computation where it is crucial to manipulate and control chains of magnetically active atoms on superconductors. Rather than directly pursuing a solution of localized magnetic moments in a bath with Bardeen-Cooper-Schrieffer pairing fields, an alternative, as demonstrated in this work, is to work in a first-principle fully many-body framework including most of the realistic correlation effects and understand the problem *before* going to a superconducting bath.

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[1] W. Meissner and B. Voigt, *Ann. Phys.* **399**, 761 (1930).  
 [2] W. de Haas, J. de Boer, and G. van den Berg, *Physica* **1**, 1115 (1934).

[3] J. Kondo, *Prog. Theor. Phys.* **32**, 37 (1964).  
 [4] J. Kondo, *Phys. Rev.* **169**, 437 (1968).  
 [5] P. W. Anderson, *Phys. Rev.* **124**, 41 (1961).

- [6] P. W. Anderson, *J. Phys. C: Solid State Phys.* **3**, 2436 (1970).
- [7] K. G. Wilson, *Rev. Mod. Phys.* **47**, 773 (1975).
- [8] A. A. Abrikosov, *Phys. Phys. Fiz.* **2**, 5 (1965).
- [9] A. A. Abrikosov, *Phys. Phys. Fiz.* **2**, 61 (1965).
- [10] H. Suhl, *Theory of Magnetism in Transition Metals* (Academic, London, 1967), pp. 116–205.
- [11] F. Patthey, B. Delley, W. D. Schneider, and Y. Baer, *Phys. Rev. Lett.* **55**, 1518 (1985).
- [12] F. Patthey, W. D. Schneider, Y. Baer, and B. Delley, *Phys. Rev. Lett.* **58**, 2810 (1987).
- [13] F. Patthey, J.-M. Imer, W.-D. Schneider, H. Beck, Y. Baer, and B. Delley, *Phys. Rev. B* **42**, 8864 (1990).
- [14] C. Laubschat, E. Weschke, C. Holtz, M. Domke, O. Strebel, and G. Kaindl, *Phys. Rev. Lett.* **65**, 1639 (1990).
- [15] E. Weschke, C. Laubschat, T. Simmons, M. Domke, O. Strebel, and G. Kaindl, *Phys. Rev. B* **44**, 8304 (1991).
- [16] D. Ehm, S. Hübner, F. Reinert, J. Kroha, P. Wölfe, O. Stockert, C. Geibel, and H. v. Löhneysen, *Phys. Rev. B* **76**, 045117 (2007).
- [17] E. Wuilloud, H. R. Moser, W. D. Schneider, and Y. Baer, *Phys. Rev. B* **28**, 7354 (1983).
- [18] J. Li, W.-D. Schneider, R. Berndt, and B. Delley, *Phys. Rev. Lett.* **80**, 2893 (1998).
- [19] V. Madhavan, W. Chen, T. Jamneala, M. F. Crommie, and N. S. Wingreen, *Science* **280**, 567 (1998).
- [20] U. Fano, *Il Nuovo Cimento* (1924–1942) **12**, 154 (1935).
- [21] U. Fano, *Phys. Rev.* **124**, 1866 (1961).
- [22] H. O. Frota and L. N. Oliveira, *Phys. Rev. B* **33**, 7871 (1986).
- [23] H. O. Frota, *Phys. Rev. B* **45**, 1096 (1992).
- [24] R. Žitko, *Phys. Rev. B* **84**, 195116 (2011).
- [25] H. Prüser, M. Wenderoth, P. E. Dargel, A. Weismann, R. Peters, T. Pruschke, and R. G. Ulbrich, *Nat. Phys.* **7**, 203 (2011).
- [26] H. Prüser, M. Wenderoth, A. Weismann, and R. G. Ulbrich, *Phys. Rev. Lett.* **108**, 166604 (2012).
- [27] K. Nagaoka, T. Jamneala, M. Grobis, and M. F. Crommie, *Phys. Rev. Lett.* **88**, 077205 (2002).
- [28] N. Knorr, M. A. Schneider, L. Diekhöner, P. Wahl, and K. Kern, *Phys. Rev. Lett.* **88**, 096804 (2002).
- [29] P. Wahl, L. Diekhöner, M. A. Schneider, L. Vitali, G. Wittich, and K. Kern, *Phys. Rev. Lett.* **93**, 176603 (2004).
- [30] D.-J. Choi, M. V. Rastei, P. Simon, and L. Limot, *Phys. Rev. Lett.* **108**, 266803 (2012).
- [31] K. von Bergmann, M. Ternes, S. Loth, C. P. Lutz, and A. J. Heinrich, *Phys. Rev. Lett.* **114**, 076601 (2015).
- [32] S. Meierott, N. Néel, and J. Kröger, *Phys. Rev. B* **91**, 201111(R) (2015).
- [33] P. Wahl, L. Diekhöner, G. Wittich, L. Vitali, M. A. Schneider, and K. Kern, *Phys. Rev. Lett.* **95**, 166601 (2005).
- [34] A. Zhao, Q. Li, L. Chen, H. Xiang, W. Wang, S. Pan, B. Wang, X. Xiao, J. Yang, J. G. Hou, and Q. Zhu, *Science* **309**, 1542 (2005).
- [35] V. Iancu, A. Deshpande, and S.-W. Hla, *Phys. Rev. Lett.* **97**, 266603 (2006).
- [36] V. Iancu, A. Deshpande, and S.-W. Hla, *Nano Lett.* **6**, 820 (2006).
- [37] L. Gao, W. Ji, Y. B. Hu, Z. H. Cheng, Z. T. Deng, Q. Liu, N. Jiang, X. Lin, W. Guo, S. X. Du, W. A. Hofer, X. C. Xie, and H.-J. Gao, *Phys. Rev. Lett.* **99**, 106402 (2007).
- [38] I. Fernández-Torrente, K. J. Franke, and J. I. Pascual, *Phys. Rev. Lett.* **101**, 217203 (2008).
- [39] U. G. E. Perera, H. J. Kulik, V. Iancu, L. G. G. V. Dias da Silva, S. E. Ulloa, N. Marzari, and S.-W. Hla, *Phys. Rev. Lett.* **105**, 106601 (2010).
- [40] T. Choi, S. Bedwani, A. Rochefort, C.-Y. Chen, A. J. Epstein, and J. A. Gupta, *Nano Lett.* **10**, 4175 (2010).
- [41] T. Komeda, H. Isshiki, J. Liu, Y.-F. Zhang, N. Lorente, K. Katoh, B. K. Breedlove, and M. Yamashita, *Nat. Commun.* **2**, 217 (2011).
- [42] A. Mugarza, C. Krull, R. Robles, S. Stepanow, G. Ceballos, and P. Gambardella, *Nat. Commun.* **2**, 490 (2011).
- [43] N. Tsukahara, S. Shiraki, S. Itou, N. Ohta, N. Takagi, and M. Kawai, *Phys. Rev. Lett.* **106**, 187201 (2011).
- [44] K. J. Franke, G. Schulze, and J. I. Pascual, *Science* **332**, 940 (2011).
- [45] A. DiLullo, S.-H. Chang, N. Baadji, K. Clark, J.-P. Klöckner, M.-H. Proscenc, S. Sanvito, R. Wiesendanger, G. Hoffmann, and S.-W. Hla, *Nano Lett.* **12**, 3174 (2012).
- [46] R. Robles, N. Lorente, H. Isshiki, J. Liu, K. Katoh, B. K. Breedlove, M. Yamashita, and T. Komeda, *Nano Lett.* **12**, 3609 (2012).
- [47] T. G. Gopakumar, F. Matino, H. Naggert, A. Bannwarth, F. Tuczek, and R. Berndt, *Angew. Chem., Int. Ed.* **51**, 6262 (2012).
- [48] T. Miyamachi, M. Gruber, V. Davesne, M. Bowen, S. Boukari, L. Joly, F. Scheurer, G. Rogez, T. K. Yamada, P. Ohresser, E. Beaurepaire, and W. Wulfhekel, *Nat. Commun.* **3**, 938 (2012).
- [49] E. Minamitani, N. Tsukahara, D. Matsunaka, Y. Kim, N. Takagi, and M. Kawai, *Phys. Rev. Lett.* **109**, 086602 (2012).
- [50] H. Kim, Y. H. Chang, S.-H. Lee, Y.-H. Kim, and S.-J. Kahng, *ACS Nano* **7**, 9312 (2013).
- [51] B. W. Heinrich, G. Ahmadi, V. L. Müller, L. Braun, J. I. Pascual, and K. J. Franke, *Nano Lett.* **13**, 4840 (2013).
- [52] M. Ternes, A. J. Heinrich, and W.-D. Schneider, *J. Phys.: Condens. Matter* **21**, 053001 (2008).
- [53] T. Komeda, *Surf. Sci.* **630**, 343 (2014).
- [54] M. Ternes, *Prog. Surf. Sci.* **92**, 83 (2017).
- [55] W. Chen, T. Jamneala, V. Madhavan, and M. F. Crommie, *Phys. Rev. B* **60**, R8529 (1999).
- [56] V. Madhavan, T. Jamneala, K. Nagaoka, W. Chen, J.-L. Li, S. G. Louie, and M. F. Crommie, *Phys. Rev. B* **66**, 212411 (2002).
- [57] P. Wahl, P. Simon, L. Diekhöner, V. S. Stepanyuk, P. Bruno, M. A. Schneider, and K. Kern, *Phys. Rev. Lett.* **98**, 056601 (2007).
- [58] A. F. Otte, M. Ternes, K. von Bergmann, S. Loth, H. Brune, C. P. Lutz, C. F. Hirjibehedin, and A. J. Heinrich, *Nat. Phys.* **4**, 847 (2008).
- [59] A. F. Otte, M. Ternes, S. Loth, C. P. Lutz, C. F. Hirjibehedin, and A. J. Heinrich, *Phys. Rev. Lett.* **103**, 107203 (2009).
- [60] N. Néel, R. Berndt, J. Kröger, T. O. Wehling, A. I. Lichtenstein, and M. I. Katsnelson, *Phys. Rev. Lett.* **107**, 106804 (2011).
- [61] J. Bork, Y.-h. Zhang, L. Diekhöner, L. Borda, P. Simon, J. Kroha, P. Wahl, and K. Kern, *Nat. Phys.* **7**, 901 (2011).
- [62] H. Prüser, P. E. Dargel, M. Bouhassoune, R. G. Ulbrich, T. Pruschke, S. Lounis, and M. Wenderoth, *Nat. Commun.* **5**, 5417 (2014).

- [63] A. Spinelli, M. Gerrits, R. Toskovic, B. Bryant, M. Ternes, and A. F. Otte, *Nat. Commun.* **6**, 10046 (2015).
- [64] D.-J. Choi, S. Guissart, M. Ormaza, N. Bachellier, O. Bengone, P. Simon, and L. Limot, *Nano Lett.* **16**, 6298 (2016).
- [65] N. Néel, J. Kröger, L. Limot, K. Palotas, W. A. Hofer, and R. Berndt, *Phys. Rev. Lett.* **98**, 016801 (2007).
- [66] N. Néel, J. Kröger, R. Berndt, T. O. Wehling, A. I. Lichtenstein, and M. I. Katsnelson, *Phys. Rev. Lett.* **101**, 266803 (2008).
- [67] N. Néel, J. Kröger, and R. Berndt, *Phys. Rev. B* **82**, 233401 (2010).
- [68] J. Kügel, M. Karolak, J. Senkpiel, P.-J. Hsu, G. Sangiovanni, and M. Bode, *Nano Lett.* **14**, 3895 (2014).
- [69] T. Knaak, M. Gruber, C. Lindström, M.-L. Bocquet, J. Heck, and R. Berndt, *Nano Lett.* **17**, 7146 (2017).
- [70] L. Limot and R. Berndt, *Appl. Surf. Sci.* **237**, 572 (2004).
- [71] T. Uchihashi, J. Zhang, J. Kröger, and R. Berndt, *Phys. Rev. B* **78**, 033402 (2008).
- [72] Q. L. Li, C. Zheng, R. Wang, B. F. Miao, R. X. Cao, L. Sun, D. Wu, Y. Z. Wu, S. C. Li, B. G. Wang, and H. F. Ding, *Phys. Rev. B* **97**, 035417 (2018).
- [73] J. P. F. LeBlanc, A. E. Antipov, F. Becca, I. W. Bulik, G. K.-L. Chan, C.-M. Chung, Y. Deng, M. Ferrero, T. M. Henderson, C. A. Jiménez-Hoyos, E. Kozik, X.-W. Liu, A. J. Millis, N. V. Prokof'ev, M. Qin, G. E. Scuseria, H. Shi, B. V. Svistunov, L. F. Tocchio, I. S. Tupitsyn, S. R. White, S. Zhang, B.-X. Zheng, Z. Zhu, and E. Gull (Simons Collaboration on the Many-Electron Problem), *Phys. Rev. X* **5**, 041041 (2015).
- [74] M. Motta, D. M. Ceperley, G. K.-L. Chan, J. A. Gomez, E. Gull, S. Guo, C. A. Jiménez-Hoyos, T. N. Lan, J. Li, F. Ma, A. J. Millis, N. V. Prokof'ev, U. Ray, G. E. Scuseria, S. Sorella, E. M. Stoudenmire, Q. Sun, I. S. Tupitsyn, S. R. White, D. Zgid, and S. Zhang (Simons Collaboration on the Many-Electron Problem), *Phys. Rev. X* **7**, 031059 (2017).
- [75] D. Vollhardt and A. I. Lichtenstein, *Eur. Phys. J. Spec. Topics* **226**, 2439 (2017).
- [76] L. Limot, J. Kröger, R. Berndt, A. Garcia-Lekue, and W. A. Hofer, *Phys. Rev. Lett.* **94**, 126102 (2005).
- [77] J. Kröger, H. Jensen, and R. Berndt, *New J. Phys.* **9**, 153 (2007).
- [78] J. Kröger, N. Néel, and L. Limot, *J. Phys.: Condens. Matter* **20**, 223001 (2008).
- [79] J. Kröger, N. Néel, A. Sperl, Y. F. Wang, and R. Berndt, *New J. Phys.* **11**, 125006 (2009).
- [80] I. Horcas, R. Fernández, J. M. Gómez-Rodríguez, J. Colchero, J. Gómez-Herrero, and A. M. Baro, *Rev. Sci. Instrum.* **78**, 013705 (2007).
- [81] J. A. Stroschio, F. Tavazza, J. N. Crain, R. J. Celotta, and A. M. Chaka, *Science* **313**, 948 (2006).
- [82] J. Lagoute, C. Nacci, and S. Fölsch, *Phys. Rev. Lett.* **98**, 146804 (2007).
- [83] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevResearch.2.023309> for spectra of the single-Co Abrikosov-Suhl-Kondo resonance without vertical offset (Figs. S1 and S2) and spectra of the single-Co  $p_z$  resonance without vertical offset (Fig. S3).
- [84] F. Donati, S. Piccoli, C. E. Bottani, and M. Passoni, *New J. Phys.* **13**, 053058 (2011).
- [85] G. Kresse and J. Hafner, *J. Phys.: Condens. Matter* **6**, 8245 (1994).
- [86] P. E. Blöchl, *Phys. Rev. B* **50**, 17953 (1994).
- [87] G. Kresse and D. Joubert, *Phys. Rev. B* **59**, 1758 (1999).
- [88] J. P. Perdew, K. Burke, and M. Ernzerhof, *Phys. Rev. Lett.* **77**, 3865 (1996).
- [89] B. Amadon, F. Lechermann, A. Georges, F. Jollet, T. O. Wehling, and A. I. Lichtenstein, *Phys. Rev. B* **77**, 205112 (2008).
- [90] M. Karolak, T. O. Wehling, F. Lechermann, and A. I. Lichtenstein, *J. Phys.: Condens. Matter* **23**, 085601 (2011).
- [91] B. Surer, M. Troyer, P. Werner, T. O. Wehling, A. M. Läuchli, A. Wilhelm, and A. I. Lichtenstein, *Phys. Rev. B* **85**, 085114 (2012).
- [92] Ph. Nozières and A. Blandin, *J. Phys. France* **41**, 193 (1980).
- [93] A. C. Hewson, *The Kondo Problem to Heavy Fermions* (Cambridge University Press, Cambridge, 1993).
- [94] P. Werner, A. Comanac, L. de' Medici, M. Troyer, and A. J. Millis, *Phys. Rev. Lett.* **97**, 076405 (2006).
- [95] P. Werner and A. J. Millis, *Phys. Rev. B* **74**, 155107 (2006).
- [96] M. Wallerberger, A. Hausoel, P. Gunacker, A. Kowalski, N. Parragh, F. Goth, K. Held, and G. Sangiovanni, *Comput. Phys. Commun.* **235**, 388 (2019).
- [97] E. Şaşıoğlu, C. Friedrich, and S. Blügel, *Phys. Rev. B* **83**, 121101 (2011).
- [98] E. Şaşıoğlu, C. Friedrich, and S. Blügel, *Phys. Rev. Lett.* **109**, 146401 (2012).
- [99] T. Ribic, E. Assmann, A. Tóth, and K. Held, *Phys. Rev. B* **90**, 165105 (2014).
- [100] E. Gorelov, T. O. Wehling, A. N. Rubtsov, M. I. Katsnelson, and A. I. Lichtenstein, *Phys. Rev. B* **80**, 155132 (2009).
- [101] A. V. Chubukov and D. L. Maslov, *Phys. Rev. B* **86**, 155136 (2012).
- [102] M. Jarrell and J. Gubernatis, *Phys. Rep.* **269**, 133 (1996).
- [103] R. K. Bryan, *Eur. Biophys. J.* **18**, 165 (1990).
- [104] R. Levy, J. LeBlanc, and E. Gull, *Comput. Phys. Commun.* **215**, 149 (2017).
- [105] A. C. Hewson, *J. Phys. Soc. Jpn.* **74**, 8 (2005).
- [106] K. Edwards and A. C. Hewson, *J. Phys.: Condens. Matter* **23**, 045601 (2011).